

```

In[9]:=  $\theta_2 = 2;$ 
Q[M_] := Block[{ $\theta_1$ ,  $\theta_2$ , c1, c2, M21, w21},
   $\theta_1 = 5 * \theta_2;$  M21 = M;
  c1 = 2 /  $\theta_1$ ; c2 = 2 /  $\theta_2$ ; w21 = 4 M21 /  $\theta_1$ ;

  {{-(2 * w21 + c1), w21, w21, 0, c1, 0, 0, 0, 0, 0},
   {0, -(w21 + c2), 0, w21, 0, c2, 0, 0, 0, 0},
   {0, 0, -(w21 + c2), w21, 0, 0, c2, 0, 0, 0},
   {0, 0, 0, -3 * c2, 0, 0, 0, c2, c2, c2},
   {0, 0, 0, 0, -w21, 0, 0, w21, 0, 0},
   {0, 0, 0, 0, 0, -w21, 0, 0, w21, 0},
   {0, 0, 0, 0, 0, 0, -w21, 0, 0, w21},
   {0, 0, 0, 0, 0, 0, 0, -c2, 0, 0},
   {0, 0, 0, 0, 0, 0, 0, 0, -c2, c2},
   {0, 0, 0, 0, 0, 0, 0, 0, 0, 0}}
];

PG1a[ $\tau$ _, M_] := Block[{Esys, U, Evalues, P,  $\theta_1$ ,  $\theta_2$ },
   $\theta_1 = 5 * \theta_2;$ 
  Esys = Eigensystem[Q[M]];
  Evalues = Esys[[1]];
  If[Abs[Evalues[[11]]] > 10-20, Print["eigenvalue 11 is not 0?"]];
  Evalues[[11]] = -1; (* eigenvalues are ordered increasingly, last one is 0. *)
  Evalues = (Exp[Evalues *  $\tau$ ] - 1) / Evalues;
  Evalues[[11]] =  $\tau$ ;
  U = Transpose[Esys[[2]]];
  P = U . DiagonalMatrix[Evalues] . Inverse[U];
  P[[1, 1]] * 2 /  $\theta_1$  + P[[1, 4]] * 2 /  $\theta_2$ 
];

PG1b[ $\tau$ _, M_] := Block[{P},
  P = MatrixExp[Q[M] *  $\tau$ ];
  (P[[1, 1]] + P[[1, 2]] + P[[1, 3]] + P[[1, 4]]) / 3
];

PG1[ $\tau$ _, M_] := PG1a[ $\tau$ , M] + PG1b[ $\tau$ , M];

```

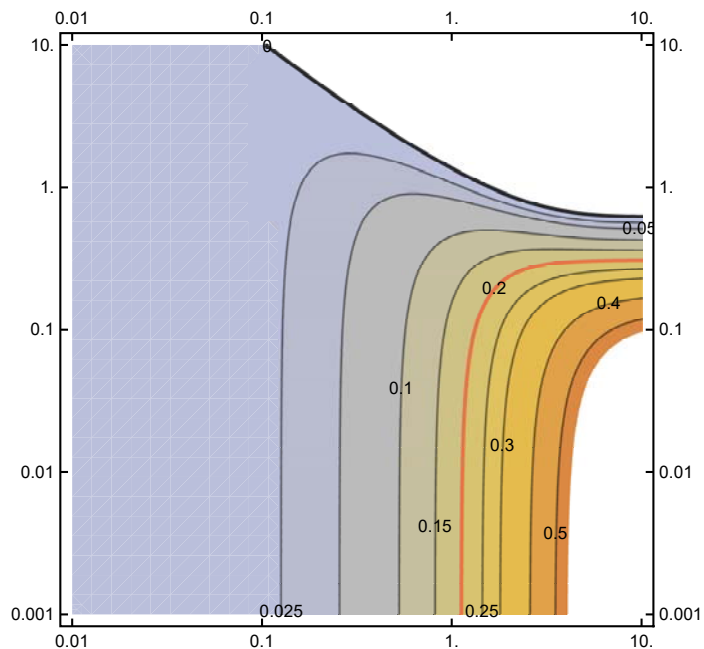
```

In[14]:= b = 10; Mmin = 0.001; Mmax = 10; τmin = 0.01; τmax = 10;
newStyle[x_] := x /. l_Line => Sequence[Opacity[.4], Thick, Red, 1]
newStyle2[x_] := x /. l_Line => Sequence[Opacity[.8], Thick, Black, 1]
ContourPlot[(PG1[b^τ, b^M] - 1/3) * 3/2,
  {τ, Log[b, τmin], Log[b, τmax]}, {M, Log[b, Mmin], Log[b, Mmax]},
  Contours -> {0, 0.025, 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 0.95},
  (* ContourStyle -> {{Red, Thin}}, *)
  BaseStyle -> {FontFamily -> "Arial", FontSize -> 9}, PlotPoints -> 30,
  ContourLabels -> All, ColorFunction -> (ColorData[{"BeachColors", "Reverse"}]),
  ContourStyle -> Thin, AspectRatio -> 1,
  (* Frame -> False, *)
  FrameTicks -> {Table[{τ, ToString[Round[b^τ, τmin]]}, {τ, Log[b, τmin], Log[b, τmax]}],
    Table[{M, ToString[Round[b^M, Mmin]]}, {M, Log[b, Mmin], Log[b, Mmax]}]}
  ] /. Tooltip[x_, 0.2] => Tooltip[newStyle[x], 0.2] /.
  Tooltip[x_, 0.7] => Tooltip[newStyle[x], 0.7] /.
  Tooltip[x_, 0] => Tooltip[newStyle2[x], 0]

ContourPlot[PG1a[b^τ, b^M], {τ, Log[b, τmin], Log[b, τmax]}, {M, Log[b, Mmin], Log[b, Mmax]},
  Contours -> {0, 0.025, 0.05, 0.1, 0.15, 0.2, 0.25, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 0.95},
  BaseStyle -> {FontFamily -> "Arial", FontSize -> 9}, PlotPoints -> 30,
  ContourLabels -> All, ColorFunction -> (ColorData[{"BeachColors", "Reverse"}]),
  ContourStyle -> Thin, AspectRatio -> 1,
  (* Frame -> False, *)
  FrameTicks -> {Table[{τ, ToString[Round[b^τ, τmin]]}, {τ, Log[b, τmin], Log[b, τmax]}],
    Table[{M, ToString[Round[b^M, Mmin]]}, {M, Log[b, Mmin], Log[b, Mmax]}]}
  ] /. Tooltip[x_, 0.2] => Tooltip[newStyle[x], 0.2] /.
  Tooltip[x_, 0.7] => Tooltip[newStyle[x], 0.7]

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Out[17]=



Out[18]=

